

Session Number: 8B
Session Title: Issues in Income Distribution
Paper Number: 2.5
Session Organizer: Edward Wolff, NYU, USA

*Paper Prepared for the 26th General Conference of The International Association
for Research in Income and Wealth, Cracow, Poland, 27th August to 2 September 2000*

**TITLE: THE CHOICE OF PRINCIPAL VARIABLES FOR COMPUTING SOME
MEASURES OF HUMAN WELL-BEING**

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Abstract

The present paper investigates the choice of principal variables for computing three measures of human well-being, namely, the Human Development Index (HDI), the Gender-Related Development Index (GDI), and the Gender Empowerment Measure (GEM). To this end, the principal components variable selection strategy considered by Jolliffe (1972, 1973) is applied to data from the 1999 Human Development Report. The empirical results show that there is statistical justification for selecting only one of the three components of each indicator. In the case of the HDI, the life expectancy index turns out to be the best choice; in the case of the GDI the best choice is the equally distributed educational attainment index; and in the case of the GEM the best choice is the index of parliamentary representation. Accordingly, it seems reasonable to compute simpler HDI, GDI and GEM based solely on the selected indicators without loss of too much information. Also, while our results support the current practice of equally weighting the three components of HDI and GDI, this is not the case for the GEM.

1. Introduction

As evidenced by a spate of recent papers on the subject, there is considerable interest in the concept and measurement of human development. See, for example, Hopkins (1991), McGillivray (1991), Dasgupta and Weale (1992), McGillivray and White (1993), Srivastavan (1994), Streeten (1994), and Pillarisetti and McGillivray (1998), among others. There are several plausible explanations for this. First, it is now widely recognized that GDP (or GNP) per capita is not a fully satisfactory measure of human well-being and that composite indicators, that incorporate more than one attribute of human well-being, are conceptually more appealing. Second, the popularization of the Basic Human Needs (BHN) approach to development in the 1970s led to the search for BHN performance indicators, which have facilitated the construction of human development indicators.¹ The BHN approach emphasizes the satisfaction of basic needs such as good nutrition, health, education, clothing and sanitation. In contrast, the traditional growth strategies emphasize increasing GDP (or GNP) per capita. Third, the annual publication of the Human Development Report (HDR) by the United Nations Development Programme (UNDP) since 1990 has raised awareness of and focused debate on the importance of the concept of human development. In fact, over the past decade the UNDP has taken the lead in conceptualizing and measuring the conditions of human development.

In the inaugural issue of the HDR, the UNDP(1990) proposed the Human Development Index (HDI) which is a composite index comprising of life expectancy, adult literacy, and real GDP per capita adjusted for purchasing power parity. The index ranges from zero to one with

¹ Some measures of BHN performance proposed by Hicks and Str incorporated in the HDI.

higher values signifying higher levels of human development. The HDI is rationalized on the grounds that human beings strive to lead long healthy lives (captured by life expectancy), to have a decent standard living (captured by real GDP per capita), and to acquire knowledge (captured by adult literacy), in which case the focus of development policy should be to expand the choices and capabilities of people in these areas. The HDI is increasingly being used as a basis for setting human development goals of many countries and more than 100 countries are already constructing national or sub-national HDIs.

In response to some of the criticisms of the earlier versions of HDI, the UNDP has continued to refine the underlying analytical framework. To this end, several improvements have been made in the methodology and quality of data used for constructing the HDI. The UNDP (1995) introduced two additional measures of human development, namely, the Gender-Related Development index (GDI) and the Gender Empowerment Measure (GEM). As we shall see in section 2 below, the GDI uses the same dimensions as the HDI except for the fact that the former takes into account gender disparities in human development. Specifically, the GDI is constructed such that countries that exhibit greater gender disparities in human development are penalized by achieving lower GDI values relative to their HDI counterparts. The GEM is a measure of the degree of women's participation in the political, economic, and professional activities. It must be pointed out that the GDI and GEM, like the HDI, lie between zero and one with greater values signifying higher levels of human development.

The HDI, GDI and GEM have the common characteristic of incorporating more than one attribute of human well-being. Although the addition of extra attributes may be appealing on conceptual grounds, it also introduces new complications with respect to the assignment of

weights to the attributes, and the added time and monetary costs of obtaining information on all attributes, among others.² Even the proponents of the HDI, GDI and GEM concede that it is impossible to come up with a comprehensive set of human development indicators. See, for example, UNDP (1999, p. 127). In fact, as pointed out by UNDP (1994, p. 91), more indicators is not necessarily better in the sense that there might be an overlap among some indicators as is the case with infant mortality which is already reflected in life expectancy. The fact that it is impossible to come up with a single composite indicator of human development that incorporates all attributes of human well-being raises the question as to whether or not there is statistical justification for including all dimensions of a particular composite indicator of human well-being. In our opinion, it is important to incorporate only attributes that add new information. Accordingly, the most parsimonious, yet informative, composite indicators of human development are recommended.

In a recent study of the HDI, Ogwang (1994) found that there is statistical justification for retaining only one of the three components of HDI. It must be noted that Ogwang's study was based on data for an earlier version of HDI obtained from the 1991 HDR. Given recent refinements in the methodology for computing the HDI as well as improvements in the quality of the underlying data, it seems reasonable to re-examine this issue using the most recently available and more reliable data for the HDI. Furthermore, to the best of our knowledge, no empirical studies have hitherto examined the issue of choice of principal variables for computing the GDI and GEM. The present paper fills in the gap by examining the choice of principal variables for

² For a discussion of the difficulties in measuring the literacy component of HDI, see Hopkins (1992, p. 1471).

computing HDI, GDI, and GEM. To this end, the principal components variable selection strategy considered by Jolliffe (1972,1973) is used to analyze data from the 1999 HDR.

The format of the rest of the paper is as follows. In section 2, the methodologies for constructing the HDI, GDI and GEM are briefly discussed. In section 3, the variable selection strategy employed is briefly described. In the penultimate section, the empirical results are presented. The concluding remarks are made in the final section.

2. Construction of the HDI, GDI and GEM

The most recent versions of HDI, GDI and GEM, reported in the 1999 HDR, are each computed as simple arithmetic means of three sub-components. The HDI is computed as a simple arithmetic mean of the life expectancy index (LEI), educational attainment index (EAI), and an index of real GDP per capita adjusted for purchasing power parity (GDPI). Prior to computing the mean, each of the three components is scaled to lie between zero and one. For further details concerning the construction of the most recent version of HDI, see UNDP (1999, pp. 159-160).

The GDI is computed as a simple arithmetic mean of an equally distributed life expectancy index (ELEI), an equally distributed educational attainment index (EEAI), and an equally distributed income index (EGDPI). Prior to computing the mean, each index is scaled to lie between zero and one. The equally distributed components take into account differential life expectancies, educational attainments and incomes of men and women as well as their differential population shares. For further details concerning construction of the most recent version of GDI, see UNDP (1999, pp. 160-161)

The GEM is computed as a simple arithmetic mean of an index of parliamentary

representation (PRI), index of administrative and managerial, and professional and technical positions (AMPTPI), and an equally distributed income index (EGDPI). Prior to computing the mean, each index is scaled to lie between zero and one. For further details concerning construction of the most recent version of GEM, see UNDP (1999, pp. 161-162).

Note that taking the arithmetic mean of the three components of each indicator amounts to assigning equal weights to these components, implying that they are equally important in that indicator. In the sections below, we will examine the issue of which component best represents the three components of each of the three human development indicators (HDI, GDI and GEM).

3. The selection strategy

Principal components analysis (PCA) technique has traditionally transform a large set of correlated variables into a smaller set of called the principal components, that account for most of the variance of variables. Since the principal components are linear combinations with mathematically determined characteristic vectors of the covariance matrix of original variables as weights, it can be argued that PCA is an arbitrary choice of weighting scheme. The first principal component captures the largest proportion of variation in the original set of variables. The second captures the largest proportion of variation which is not accounted for by the first component, and so on. For a set of k variables, the maximum number of principal components which can be extracted is equal to k . However, if the k variables are

few principal components capture most of the variation. The proportion attributed to a particular principal component is obtained by dividing the characteristic root by the sum of all the characteristic roots. Du (1993) provides a good introduction to PCA.

In principle, the high inter-correlations among the components of composite indicators could be exploited to construct new composite indicators which are, in fact, first principal components of the original components and then scaling them to lie within the desired range. A drawback of this approach is that information on all the components is required since each principal component is a linear combination of all the constituent variables.³

Recently, PCA has also served as a useful tool for selecting a few variables among a wider set of correlated variables. The technique used in the present paper is PCA method of Jolliffe (1972, p. 164; 1973, p. 22), which is recommended by Jolliffe (1972). The retention of best subsets of variables is considered important, which is the case in the present study. Essentially, the method involves first selecting the variable with the highest correlation with the first principal component. This is followed by selecting the variable which has the highest correlation with the second principal component. The stage selection process is limited only to those variables that are not selected in the first stage selection process. This procedure is continued until the required number of variables is selected. Jolliffe (1972, p. 171) recommended that the number of variables selected should be equal to the number of principal components associated with the characteristic roots.

³ See, for example, Ram (1982) and UNDP (1993, pp. 109-110).

correlation matrices of variables which are greater than 0.70. If the variables is used, the number of variables to be selected is equal to characteristic roots of the covariance matrix which are greater average of the characteristic roots associated with the covariance principal components literature. See Dunteman (1989, p. 22) for further

4. Empirical Results

The empirical results presented in this section are based on the available data taken from the 1999 HDR. The data for the HDI relate those for the GDI and GEM pertain to 143 and 102 countries, respectively. The number of countries is dictated by the availability of data as reported

To provide some insights into the degree of association among the three components of each of HDI, GDI, and GEM, the covariance moment correlation coefficients and the Spearman's rank correlation reported in Table 1. Evidence of strong positive correlation among each human development indicator is apparent from the table. These are exhibited by the three GEM components.

Table 1 here

Since the selection strategy employed here requires knowledge and characteristic vectors of the covariance matrices of the three indicator, the covariances and the associated characteristic roots

HDI components are reported in Table 2. Similar data for the GDI are in Table 3 and Table 4, respectively.⁴ It can be seen from the entries in Table 2 that the first principal component accounts for approximately 85 per cent of the variation in the three variables. Clearly, the first principal component contains most of the information embedded in the three components of HDI.

The components of the characteristic vector associated with the first principal component of the three HDI components show that the first principal component could be computed as $0.564 \text{ (LEI)} + 0.620 \text{ (EAI)} + 0.546 \text{ (GDPI)}$. However, this method of computing all the three components, which can be expensive to compute, is not ideal. Since the components of the characteristic vector associated with the first principal component do not sum to unity, the first principal component HDI series will not be a unit root process without further transformation.⁵ Another notable feature of the first principal component weights attached to the three HDI components is that they are not equal, which is consistent with the equal weighting scheme adopted by

⁴The present study uses the covariance matrix of variables rather than the correlation matrix since the units of measurement of the three components of HDI are reasonably commensurate, as suggested in the principal component analysis (see Morrison, 1967, p. 223).

⁵For the weights to sum to unity, the weight attached to each component should be divided by the sum of all the weights in each case.

of the HDI in the 1999 HDR. It is also easy to verify from the entries characteristic root is greater than 0.708, suggesting that only one is retained for purposes of computing a simpler HDI.

Table 2 here

Since the decision as to which of the three variables should be retained is based on the information on the correlations (or loadings) between the variables and the principal components, these correlations are also reported in Table 2. It can be seen from the table that the life expectancy index (LEI) has the highest correlation with the first principal component. Accordingly, it can be concluded, based on the Kaiser-Meyer-Olkin selection criterion, that the life expectancy index (LEI) is the best variable to use in a series based solely on the LEI would be cheaper to compute without loss of statistical information. In fact, the product moment correlation and rank correlation between the HDI and LEI are 0.934 and 0.944, respectively, which are very close to a near perfect positive correlation.

Table 3 shows the results of PCA of the three GDI components. The results in the table are in order. First, the first principal component accounts for 94.4 percent of the variation in the three components of GDI. The first two principal components account for approximately 94 percent of the variation in the three variables. The first principal component contains most of the statistical information. Second, the components of the characteristic vector of the first principal component of the three GDI components show that the

GDI series could be computed as 0.542 (ELEI) + 0.644 (EEAI) + 0.539 (EGDPI). necessitates data for computing all the three components, which Furthermore, since the components of the characteristic vector principal component do not sum to unity, the first principal component between zero and one without further transformation. Third, the weights attached to the three GDI components are approximately with the equal weighting scheme adopted by the UNDP in the 1999 HDR. Fourth, it is also easy to verify from the entries in Table 3 that the first principal component root is greater than 0.708 suggesting that only one of the three purposes of computing a simpler GDI. An inspection of the correlations between the three GDI components and the principal components and application of the aforementioned method indicates that the selected variable should be the equally distributed index (EEAI). Thus, a simpler GDI series based solely on EEA I would be a loss of too much information. In fact, the product moment correlation coefficients between the GDI and EEA I are 0.924 and 0.907 , respectively, both indicating near perfect positive correlation. We also note that the sole indicator for constructing the GDI in the 1999 HDR, there would have increased from 143 to 145.

Table 3 here

Table 4 shows the results of PCA of the three GEM components. The results in the table are worthy of mention. First, the first principal component

65 percent of the variation in the three GEM components. The first two components account for approximately 85 percent of the variation in the three components. With the HDI and GDI, the first principal component contains most of the information embedded in the three GEM components. Second, the characteristic vectors associated with the first principal component and the other two components show that the first principal component GEM series can be expressed as $0.571(\text{AMPTPI}) + 0.388(\text{AMPTPI}) + 0.481(\text{EGDPI})$. However, this also necessitates data for all three components, which can be expensive to collect. Furthermore, since the characteristic vector associated with the first principal component is not orthogonal to the other two, the first principal component GEM series will not lie between zero and one after a linear transformation. Third, unlike in the cases of the HDI and GDI, the weights attached to the three GEM components are not approximately equal, in conformity with the equal weighting scheme adopted by the UNDP for the GEM in the 1999 HDR. Fourth, it is also easy to verify from the entries of the characteristic roots that the largest characteristic root is greater than 0.708 suggesting that only one component should be retained for purposes of computing a simpler GEM. An inspection of the variables and the principal components and application of the Kaiser-Meyer-Olkin criterion shows that the selected variable should be the index of human development (HDI) or the index of economic freedom (EF) or the index of political rights (PRI). Thus, a simpler GEM series based solely on the EF can be computed without loss of too much information. In fact, the product-moment correlation coefficients between the GEM and PRI are 0.857 and 0.857.

are very close to one indicating near perfect positive correlation. If PRI been used as the sole indicator for constructing the GEM in the countries ranked would have increased from 102 to 164.

Table 4 here

5. Concluding Remarks

In this paper, the principal components variable selection strategy of Jolliffe (1972, 1973) is used to investigate the choice of principal variables for human development indicators, namely, the HDI, GDI and GEM using the principal component method (PCR). The life expectancy index (LEI) turns out to be the best choice for the HDI; the simplified HDI; in the case of the GDI, the equally distributed education index (EEAI) turns out to be the best choice; and in the case of the GEM the principal component representation (PRI) is the best choice. Furthermore, the correlation between the indicator and the best variable for constructing that indicator is high. Accordingly, it seems reasonable to compute simpler HDI, GDI and GEM using the selected indicators without loss of too much information. Our results challenge the current practice of equally weighting the three GEM components. Finally, it must be pointed out that our discussion concerning the choice of indicators is based purely on the analysis of the internal structures of the data and does not preclude the use of other criteria for inclusion of other

variables to these indicators.

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Table 1
Covariances and correlations among the three components of HDI, GDI and GEM

Development indicator		Covariance	Pearson's correlation	Spearman's correlation
HDI	LEI and EAI	0.029	0.779	0.772
	LEI and GDPI	0.027	0.809	0.858
	EAI and GDPI	0.027	0.73	0.733
GDI	ELEI and EEAI	0.03	0.776	0.788
	ELEI and EGDPI	0.027	0.811	0.872
	EEAI and EGDPI	0.03	0.761	0.787
GEM	PRI and AMPTPI	0.018	0.477	0.493
	PRI and EGDPI	0.019	0.438	0.365
	EGDPI and AMPTPI	0.01	0.319	0.415

Table 2
Results of PCA of the three HDI components using their covariance matrix

	Principal component		
	First	Second	Third
Characteristic root	0.090849	0.01024	0.00605
Percentage of variance explained individually	81.8	6.6	5.6
Percentage of variance explained cumulatively	81.8	94.4	100
Characteristic vectors*	0.564 LEI EAI GDPI	0.262 -0.761 -0.594	0.783 -0.192 -0.591
Correlation coefficient with*	0.931 LEI EAI GDPI	-0.145 0.380 -0.332	0.334 -0.074 -0.254

* LEI, EAI, and GDPI denote the life expectancy index, the educational attainment index, and the index of real GDP per capita adjusted for purchasing power parity, respectively.

Table 3
Results of PCA of the three GDI components using their covariance matrix

	Principal component		
	First	Second	Third
Characteristic root	0.09656	0.01007	0.00631
Percentage of variance explained	85.5	8.9	5.6
Percentage of variance explained	85.5	94.4	100
Characteristic vectors*	0.542 EELI EEAI EGDPI	0.388 EELI 0.761 -0.519	-0.745 0.072 0.663
Correlation coefficient with*	0.922 EELI EEAI EGDPI	-0.223 EELI 0.356 -0.284	-0.324 0.027 0.287

* EELI, EEAI, and EGDPI denote the equally distributed life expectancy index, the equally distributed educational attainment index, and the equally distributed income index, respectively.

Table 4
Results of PCA of the three GEM components using their covariance matrix

	Principal component		
	First	Second	Third
Characteristic root	0.075832	0.0241	0.017712
Percentage of variance explained	61.5	20.4	15.1
Percentage of variance explained	61.5	81.9	100
Characteristic vectors*	0.786 PRI 0.388 AMPTPI 0.481 EGDPI	0.450 PRI -0.174 AMPTPI 0.876 EGDPI	-0.424 PRI 0.905 AMPTPI -0.038 EGDPI
Correlation coefficient with*	0.924 PRI 0.635 AMPTPI 0.698 EGDPI	-0.297 PRI -0.165 AMPTPI 0.716 EGDPI	-0.241 PRI 0.737 AMPTPI -0.027 EGDPI

* PRI, AMPTPI, and EGDPI denote the index of parliamentary representation, the index of administrative and managerial, and technical positions, and the equally distributed income index, respectively.